

№	Решение без использования программирования	Ответ
1.	<p>A recursion tree for F(8). The root is F(8), which branches into F(7), F(4), and F(2). F(7) branches into F(6), F(3), and F(2). F(6) branches into F(5), F(3), and F(2). F(5) branches into F(3) and F(2). F(3) branches into F(2) and F(1). F(2) branches into F(1) and F(0). The leaf nodes are marked with asterisks (*).</p>	13
2.	<p>A recursion tree for F(2). The root is F(2), which branches into F(3), F(4), and F(5). F(3) branches into F(4) and F(6). F(4) branches into F(6) and F(6). F(5) branches into F(4) and F(5). The leaf nodes are marked with numbers: 2, 3, 4, 6, 6, 4, 5.</p>	30
3.	<p>A recursion tree for F(7). The root is F(7), which branches into F(6), F(3), and F(2). F(6) branches into F(5), F(3), and F(2). F(5) branches into F(4), F(2), and F(1). F(4) branches into F(3), F(2), and F(1). F(3) branches into F(2) and F(1). F(2) branches into F(1) and F(0). The leaf nodes are marked with numbers: 7, 6, 5, 4, 3, F(2), F(1), F(1), 3, 3.</p>	7654333
4.	<p>A recursion tree for F(4). The root is F(4), which branches into F(8), F(5), and F(6). F(8) branches into F(10), F(6), and F(7). F(5) branches into F(10), F(6), and F(7). F(6) branches into F(10), F(6), and F(7). The leaf nodes are marked with numbers: 4, 4, 8, 5, 5, 10, 6, 7, 6.</p>	29
5.	<p>A recursion tree for F(5). The root is F(5), which branches into F(4), F(2), and F(2). F(4) branches into F(3), F(2), and F(1). F(3) branches into F(2), F(1), and F(0). F(2) branches into F(1) and F(0). F(1) branches into F(0) and F(-1). The leaf nodes are marked with numbers: 5, 5, 4, 4, 3, 3, 2, 1, 0, 2, 1, 2, 2.</p>	17

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6.	<p>A recursion tree for F(5). The root is F(5), which branches into F(6), F(7), and F(10). F(6) branches into F(7), F(8), and F(12). F(7) branches into F(8) and F(12). F(8) branches into F(12) and F(12). The leaf nodes are marked with numbers: 5, 6, 7, 8, 12, 6, 7, 10, 5.</p>	571275
7.	<p>A recursion tree for F(11). The root is F(11), which branches into F(10), F(5), and F(9). F(10) branches into F(9), F(5), and F(8). F(9) branches into F(8) and F(8). F(8) branches into F(8) and F(8). The leaf nodes are marked with numbers: 11, 10, 9, 5, 8, 10, 5, 9, 11.</p>	105109
8.	<p>A recursion tree for F(4). The root is F(4), which branches into F(5) and F(8). F(5) branches into F(6) and F(10). F(6) branches into F(10) and F(10). F(8) branches into F(10) and F(10). The leaf nodes are marked with numbers: 4, 5, 6, 10, 5, 8, 4.</p>	45610584
9.	<p>A recursion tree for F(14). The root is F(14), which branches into G(13), F(11), G(10), F(8), G(7), F(5), G(4), F(2), G(1), F(0). The leaf nodes are marked with asterisks (*).</p>	11
10.	<p>A recursion tree for F(1). The root is F(1), which branches into G(2), F(4), G(5), F(10), G(11), F(22), G(23), F(46). The leaf nodes are marked with numbers: 1, 4, 10, 22, 46, 23, 11, 5, 2.</p>	70

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11.		282044
12.		33
13.		191685

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14.		78
15.		141365

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16.	<pre>function F(n: integer): integer; begin if n <= 3 then F:= n - 1 else F:= F(n-3) + F(n-2) + F(n-1); end; begin writeln(F(22)); end.</pre>	<pre>def F(n): if n <= 3: f = n - 1 else: f = F(n-3) + F(n-2) + F(n-1) return f print(F(22))</pre>	187427
17.	<pre>function F(n: integer): integer; begin if n <= 2 then F:= 1 else F:= F(n-2)*(n-1) + F(n-1)*n; end; begin writeln(F(9)); end.</pre>	<pre>def F(n): if n <= 2: f = 1 else: f = F(n-2)*(n-1) + F(n-1)*n return f print(F(9))</pre>	641075
18.	<pre>function F(n: integer): integer; begin if n <= 2 then F:= 2 * n else F:= 2 * F(n-1) + 4 * F(n-2); end; begin writeln(F(12)); end.</pre>	<pre>def F(n): if n <= 2: f = 2 * n else: f = 2 * F(n-1) + 4 * F(n-2) return f print(F(12))</pre>	589824
19.	<pre>function F(n: integer): integer; begin if n = 1 then F:= 1 else if n = 2 then F:= 3 else F:= F(n-1) + F(n-2) * (n-1); end; begin writeln(F(10)); end.</pre>	<pre>def F(n): if n == 1: f = 1 elif n == 2: f = 3 else: f = F(n-1) + F(n-2) * (n-1) return f print(F(10))</pre>	12824
20.	<pre>function F(n: integer): integer; begin if n = 1 then F:= 1 else if n = 2 then F:= 3 else F:= F(n - 1) * F(n - 2) + n; end; begin writeln(F(7)); end.</pre>	<pre>def F(n): if n == 1: f = 1 elif n == 2: f = 3 else: f = F(n - 1) * F(n - 2) + n return f print(F(7))</pre>	413747
21.	<pre>function F(n:integer): integer; forward; function G(n:integer): integer; forward; function F(n: integer): integer; begin if n = 1 then F:= 1 else F:= G(n) + G(n - 1); end; function G(n: integer): integer; begin if n = 1 then G:= 1 else G:= F(n - 1) * n; end; begin writeln(F(8)); end.</pre>	<pre>def F(n): if n == 1: f = 1 else: f = G(n) + G(n - 1) return f def G(n): if n == 1: g = 1 else: g = F(n - 1) * n return g print(F(8))</pre>	148329

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22.	<pre>function F(n:integer): integer; forward; function G(n:integer): integer; forward; function F(n: integer): integer; begin if n = 1 then F:= 1 else F:= G(n) * G(n - 1); end; function G(n: integer): integer; begin if n = 1 then G:= 1 else G:= F(n - 1) + n; end; begin writeln(G(7)); end.</pre>	<pre>def F(n): if n == 1: f = 1 else: f = G(n) * G(n - 1) return f def G(n): if n == 1: g = 1 else: g = F(n - 1) + n return g print(G(7))</pre>	413747
23.	<pre>function F(n:integer): integer; forward; function G(n:integer): integer; forward; function F(n: integer): integer; begin if n = 1 then F:= 1 else F:= G(n) * n + G(n-1) * (n-1); end; function G(n: integer): integer; begin if n=1 then G:=2 else G:= F(n - 1) - 1; end; begin writeln(F(9)); end.</pre>	<pre>def F(n): if n == 1: f = 1 else: f = G(n) * n + G(n-1) * (n-1) return f def G(n): if n == 1: g = 2 else: g = F(n - 1) - 1 return g print(F(9))</pre>	270864
24.	<pre>function F(n:integer): integer; forward; function G(n:integer): integer; forward; function F(n: integer): integer; begin if n = 1 then F:= 2 else F:= G(n) * G(n - 1) + n; end; function G(n: integer): integer; begin if n= 1 then G:= 2 else G:= F(n - 1) * n; end; begin writeln(G(5)); end.</pre>	<pre>def F(n): if n == 1: f = 2 else: f = G(n) * G(n - 1) + n return f def G(n): if n == 1: g = 2 else: g = F(n - 1) * n return g print(G(5))</pre>	73820
25.	<pre>function F(n:integer): integer; forward; function G(n:integer): integer; forward; function F(n: integer): integer; begin if n = 1 then F:= 2 else F:= G(n) * (n-1) + G(n-1) * n; end; function G(n: integer): integer; begin if n = 1 then G:= 1 else G:= F(n - 1) * (n - 1); end; begin writeln(F(6)); end.</pre>	<pre>def F(n): if n == 1: f = 2 else: f = G(n)*(n-1) + G(n-1)*n return f def G(n): if n == 1: g = 1 else: g = F(n - 1) * (n - 1) return g print(F(6))</pre>	105770

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26.	<pre>function F(n:integer): integer; forward; function G(n:integer): integer; forward; function F(n: integer): integer; begin if n = 1 then F:= 1 else F:= F(n-1) * (n+2) - G(n-1); end; function G(n: integer): integer; begin if n = 1 then G:= 1 else G:= F(n - 1) + G(n - 1) * n; end; begin writeln(G(8)); end.</pre>	<pre>def F(n): if n == 1: f = 1 else: f = F(n-1) * (n+2) - G(n-1) return f def G(n): if n == 1: g = 1 else: g = F(n - 1) + G(n - 1) * n return g print(G(8))</pre>	181440
27.	<pre>function F(n:integer): integer; forward; function G(n:integer): integer; forward; function F(n: integer): integer; begin if n = 1 then F:= 1 else F:= F(n-1) * (n+1) - G(n-1); end; function G(n: integer): integer; begin if n = 1 then G:= 0 else G:= F(n - 1) + G(n - 1); end; begin writeln(F(8)); end.</pre>	<pre>def F(n): if n == 1: f = 1 else: f = F(n-1) * (n+1) - G(n-1) return f def G(n): if n == 1: g = 0 else: g = F(n - 1) + G(n - 1) return g print(F(8))</pre>	136371
28.	<pre>function F(n:integer): integer; forward; function G(n:integer): integer; forward; function F(n: integer): integer; begin if n = 1 then F:= 3 else F:= F(n - 1) * G(n - 1); end; function G(n: integer): integer; begin if n = 1 then G:= 1 else G:= F(n - 1) + G(n - 1); end; begin writeln(G(7)); end.</pre>	<pre>def F(n): if n == 1: f = 3 else: f = F(n - 1) * G(n - 1) return f def G(n): if n == 1: g = 1 else: g = F(n - 1) + G(n - 1) return g print(G(7))</pre>	166087
29.	<pre>function F(n:integer): integer; forward; function G(n:integer): integer; forward; function F(n: integer): integer; begin if n = 1 then F:= 1 else F:= F(n - 1) * G(n - 1) * n; end; function G(n: integer): integer; begin if n = 1 then G:= 1 else G:= F(n - 1) + G(n - 1) + n; end; begin writeln(F(5)); end.</pre>	<pre>def F(n): if n == 1: f = 1 else: f = F(n - 1) * G(n - 1) * n return f def G(n): if n == 1: g = 1 else: g = F(n - 1) + G(n - 1) + n return g print(F(5))</pre>	159840

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30.	<pre>function F(n:integer): integer; forward; function G(n:integer): integer; forward; function F(n: integer): integer; begin if n = 1 then F:=1 else F:= F(n - 1) * (G(n - 1) + n); end; function G(n: integer): integer; begin if n=1 then G:=2 else G:= F(n - 1) + G(n - 1) + n; end; begin writeln(G(5)); end.</pre>	<pre>def F(n): if n == 1: f = 1 else: f = F(n - 1) * (G(n - 1) + n) return f def G(n): if n == 1: g = 2 else: g = F(n - 1) + G(n - 1) + n return g print(G(5))</pre>	565
31.	<pre>function F(n: integer): integer; begin if n = 1 then F:= -2 else if n = 2 then F:= -1 else F:= F(n - 1) * F(n - 2); end; begin writeln(F(9)); end.</pre>	<pre>def F(n): if n == 1: f = -2 elif n == 2: f = -1 else: f = F(n-1) * F(n-2) return f print(F(9))</pre>	8192
32.	<pre>function F(n: integer): integer; begin if n = 1 then F:= 1 else if (n mod 3=0) then F:= F(n - 1) * (n - 1) else F:= F(n - 1) * (n + 1); end; begin writeln(F(8)); end.</pre>	<pre>def F(n): if n == 1: f = 1 elif n % 3 == 0: f = F(n-1) * (n-1) else: f = F(n-1) * (n+1) return f print(F(8))</pre>	64800
33.	<pre>function F(n: integer): integer; begin if n <= 2 then F:= n else if (n mod 2=1) then F:= F(n - 1) * n + F(n - 2) else F:= F(n - 1) + F(n - 2) * (n - 1); end; begin writeln(F(10)); end.</pre>	<pre>def F(n): if n <= 2: f = n elif n % 2 == 1: f = F(n-1) * n + F(n-2) else: f = F(n-1) + F(n-2) * (n-1) return f print(F(10))</pre>	36851
34.	<pre>function F(n: integer): integer; begin if n <= 2 then F:= n else if (n mod 3=0) then F:= F(n - 1) * (n - 1) + F(n - 2) else F:= F(n - 1) + F(n - 2) * (n - 2); end; begin writeln(F(11)); end.</pre>	<pre>def F(n): if n <= 2: f = n elif n % 3 == 0: f = F(n-1) * (n-1) + F(n-2) else: f = F(n-1) + F(n-2) * (n-2) return f print(F(11))</pre>	92514

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35.	<pre>function F(n: integer): integer; begin if n = 1 then F:=-1 else if n = 2 then F:= 1 else begin if (n mod 2=1) then F:= F(n - 1) * F(n - 2) else F:= F(n - 1) + F(n - 3); end; end; begin writeln(F(14)); end.</pre>	<pre>def F(n): if n == 1: f = -1 elif n == 2: f = 1 elif n % 2 == 1: f = F(n-1) * F(n-2) else: f = F(n-1) + F(n-3) return f print(F(14))</pre>	7120
36.	<pre>function F(n: integer): integer; begin if n = 1 then F:=-1 else if n = 2 then F:= 1 else begin if (n mod 3=0) then F:= F(n - 1) * F(n - 2) + n else F:= F(n - 2) + F(n - 3); end; end; begin writeln(F(17)); end.</pre>	<pre>def F(n): if n == 1: f = -1 elif n == 2: f = 1 elif n % 3 == 0: f = F(n-1) * F(n-2) + n else: f = F(n-2) + F(n-3) return f print(F(17))</pre>	34641
37.	<pre>function F(n: integer): integer; forward; function G(n: integer): integer; forward; function F(n: integer): integer; begin if n <= 2 then F:= n else F:= G(n - 1) + F(n - 2); end; function G(n: integer): integer; begin if n <= 2 then G:= n else G:= F(n - 1) * n + G(n - 2); end; begin writeln(F(10)); end.</pre>	<pre>def F(n): if n <= 2: f = n else: f = G(n-1) + F(n-2) return f def G(n): if n <= 2: g = n else: g = F(n-1) * n + G(n-2) return g print(F(10))</pre>	5879
38.	<pre>function F(n: integer): integer; forward; function G(n: integer): integer; forward; function F(n: integer): integer; begin if n = 1 then F:= 2 else if n = 2 then F:= 1 else F:= G(n - 1) * n + F(n - 2); end; function G(n: integer): integer; begin if n = 1 then G:= 1 else if n = 2 then G:= 2 else G:= F(n - 1) - G(n - 2); end; begin writeln(F(12)); end.</pre>	<pre>def F(n): if n == 1: f = 2 elif n == 2: f = 1 else: f = G(n - 1) * n + F(n - 2) return f def G(n): if n == 1: g = 1 elif n == 2: g = 2 else: g = F(n - 1) - G(n - 2) return g print(F(12))</pre>	6497

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39.	<pre>function F(n: integer): integer; forward; function G(n: integer): integer; forward; function F(n: integer): integer; begin if n = 1 then F:= 1 else if n = 2 then F:= 3 else F:= G(n - 1)*(n-1) + F(n - 2); end; function G(n: integer): integer; begin if n = 1 then G:= 2 else if n = 2 then G:= 1 else G:= F(n - 2) * n + G(n - 1); end; begin writeln(F(9)); end.</pre>	<pre>def F(n): if n == 1: f = 1 elif n == 2: f = 3 else: f = G(n - 1)*(n-1) + F(n - 2) return f def G(n): if n == 1: g = 2 elif n == 2: g = 1 else: g = F(n - 2) * n + G(n - 1) return g print(F(9))</pre>	16393
40.	<p>Необходимо определить $F(2023) / F(2020)$ для функции: $F(n) = F(n - 1) \times n$, при $n > 1$. Для этого $F(2020)$ определяем как исходный элемент рекурсивной функции равным 1.</p> <pre>function F(n:integer):int64; begin if n=2020 then F:=1 else F:=F(n-1)*n; end; begin writeln(F(2023)/F(2020)); //можно и так: writeln(F(2023)); end.</pre>	<pre>def F(n): if n == 2020: f = 1 else: f = F(n - 1) * n return f print(int(F(2023) / F(2020))) # можно и так: print(F(2023))</pre>	8266912626
41.	<p>Необходимо определить $F(2002) / F(1999)$ для функции: $F(n) = F(n - 1) \times (n - 1)$, при $n > 1$. Задаём $F(1999) = 1$ как исходный элемент рекурсивной функции.</p> <pre>function F(n:integer):int64; begin if n=1999 then F:=1 else F:=F(n-1)*(n-1); end; begin writeln(F(2002)/F(1999)); //можно и так: writeln(F(2002)); end.</pre>	<pre>def F(n): if n == 1999: f = 1 else: f = F(n - 1) * (n - 1) return f print(int(F(2002) / F(1999))) # можно и так: print(F(2002))</pre>	7999998000
42.	<p>Необходимо определить $F(123456799) - F(123456733)$ для функции: $F(n) = F(n - 1) + (n - 2)$, при $n > 2$. Задаём $F(123456733) = 0$ как исходный элемент рекурсивной функции.</p> <pre>function F(n:integer):int64; begin if n=123456733 then F:=0 else F:=F(n-1)+(n-2); end; begin writeln(F(123456799)-F(123456733)); //можно и так: writeln(F(123456799)); end.</pre>	<pre>def F(n): if n == 123456733: f = 0 else: f = F(n - 1) + (n - 2) return f print(F(123456799) - F(123456733)) # можно и так: print(F(123456799))</pre>	8148146457
43.	<p>Необходимо определить $F(1024) / F(1018)$ для функции: $F(n) = F(n - 2) \times n$, при $n > 2$. Задаём $F(1018) = 1$ как исходный элемент рекурсивной функции.</p> <pre>function F(n:integer):int64; begin if n=1018 then F:=1 else F:=F(n-2)*n; end; begin writeln(F(1024)/F(1018)); //можно и так: writeln(F(1024)); end.</pre>	<pre>def F(n): if n == 1018: f = 1 else: f = F(n - 2) * n return f print(int(F(1024) / F(1018))) # можно и так: print(F(1024))</pre>	1067458560

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44.	<p>Необходимо определить $F(112233469) - F(112233345)$ для функции: $F(n) = F(n - 2) + (n + 1)$, при $n > 2$. Задаём $F(112233345) = 0$ как исходный элемент рекурсивной функции.</p> <pre>function F(n:integer):int64; begin if n=112233345 then F:=0 else F:=F(n-2)+(n+1); end; begin writeln(F(112233469)-F(112233345)); //можно и так: writeln(F(112233469)); end.</pre>	<pre>def F(n): if n == 112233345: f = 0 else: f = F(n - 2) + (n + 1) return f print(F(112233469) - F(112233345)) # можно и так: print(F(112233469))</pre>	6958471358
45.	<p>Необходимо определить $F(987654299) - F(987654259)$ для функции: $F(n) = F(n - 2) + (n \text{ div } 2)$, при $n > 2$. Задаём $F(987654259) = 0$ как исходный элемент рекурсивной функции.</p> <pre>function F(n:integer):int64; begin if n=987654259 then F:=0 else F:=F(n-2)+(n div 2); end; begin writeln(F(987654299)-F(987654259)); //можно и так: writeln(F(987654299)); end.</pre>	<pre>def F(n): if n == 987654259: f = 0 else: f = F(n - 2) + (n // 2) return f print(F(987654299) - F(987654259)) # можно и так: print(F(987654299))</pre>	9876542790
46.	<p>Необходимо определить $F(1359) / G(1355)$ для функций: $F(n) = G(n - 2) \times n$, $G(n) = F(n) \times (n - 2)$ при $n > 2$. Задаём $G(1355) = 1$ как исходный элемент рекурсивной функции.</p> <pre>function F(n:integer):int64;forward; function G(n:integer):int64;forward; function G(n:integer):int64; begin if n=1355 then G:=1 else G:=F(n)*(n-2); end; function F(n:integer):int64; begin F:=G(n-2)*n; end; begin writeln(F(1359)/G(1355)); //можно и так: writeln(F(1359)); end.</pre>	<pre>def G(n): if n == 1355: g = 1 else: g = F(n) * (n - 2) return g def F(n): return G(n - 2) * n print(int(F(1359) / G(1355))) # можно и так: print(F(1359))</pre>	2498840865
47.	<p>Необходимо определить $G(135924680) - G(135924608)$ для функций: $F(n) = G(n - 1) + n$, $G(n) = F(n - 1) + (n - 1)$ при $n > 1$. Задаём $G(135924608) = 0$ как исходный элемент рекурсивной функции.</p> <pre>function F(n:integer):int64;forward; function G(n:integer):int64;forward; function G(n:integer):int64; begin if n=135924608 then G:=0 else G:=F(n-1)+(n-1); end; function F(n:integer):int64; begin F:=G(n-1)+n; end; begin writeln(G(135924680)-G(135924608)); //можно и так: writeln(G(135924680)); end.</pre>	<pre>def G(n): if n == 135924608: g = 0 else: g = F(n - 1) + (n - 1) return g def F(n): return G(n - 1) + n print(G(135924680) - G(135924608)) # можно и так: print(G(135924680))</pre>	9786574368

№	Решение на языке PascalABC.NET	Решение на языке Python	Отеет
48.	<p>Необходимо определить $G(31416201) - F(31415900)$ для функций: $F(n) = G(n - 2) + (n - 1)$, $G(n) = F(n - 1) + (n - 2)$ при $n > 2$. Задаём $F(31415900) = 0$ как исходный элемент рекурсивной функции.</p> <pre>function F(n:integer):int64;forward; function G(n:integer):int64;forward; function F(n:integer):int64; begin if n=31415900 then F:=0 else F:=G(n-2)+(n-1); end; function G(n:integer):int64; begin G:=F(n-1)+(n-2); end; begin writeln(G(31416201)-F(31415900)); //можно и так: writeln(G(31416201)); end.</pre>	<pre>def F(n): if n == 31415900: f = 0 else: f = G(n - 2) + (n - 1) return f def G(n): return F(n - 1) + (n - 2) print(G(31416201) - F(31415900)) # можно и так: print(G(31416201))</pre>	6314625999